

# G.C.E.(O.L.) Support Seminar - 2016

**Mathematics I**

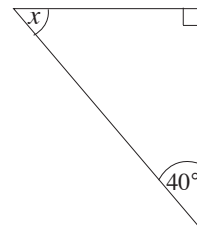
*Two hours*

## Part A

Answer **all** questions on this paper itself. Each question carries 02 marks.

1. Express  $\log_8 64 = 2$  in index form.

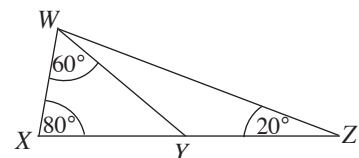
2. Find the value of  $x$  based on the information in the figure.



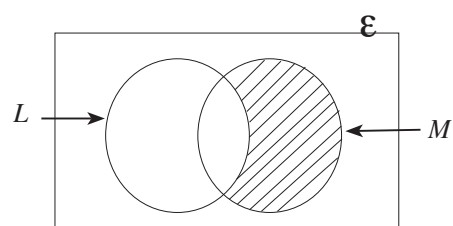
3. Mala gives Rs. 540 000 as a loan at a monthly simple interest rate of 2%. How much interest does Mala receive for 6 months?

4. Factorize :  $x^2 + 5x + 4$

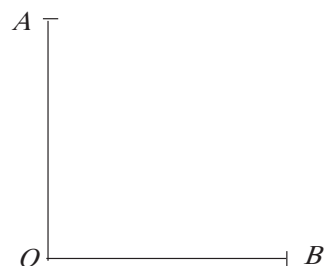
5. If  $XYZ$  is a straight line, name two sides which are equal, based on the information in the figure.



6. Write down the shaded region in the Venn diagram using set notation.



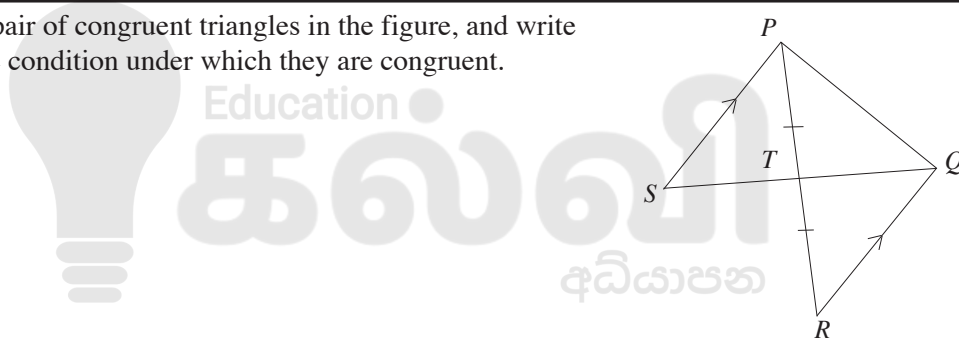
7.  $O$  and  $B$  in the figure are two points on a horizontal ground and  $OA$  is a vertical pillar. The angle of elevation of  $A$  when observed from the point  $B$  is  $60^\circ$ . What is the magnitude of the angle of depression of  $B$  when observed from  $A$ ?



8. If  $S$  is the sample space of a random experiment with equally likely outcomes and  $A$  is an event of it such that  $P(A) = \frac{1}{5}$  and  $n(A) = 8$ , then find  $n(S)$ .

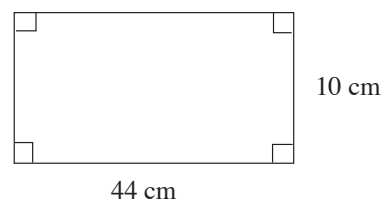
9. Find the inter-quartile range of the group of data 2, 2, 3, 3, 5, 6, 7, 8, 9, 11, 13.

10. Name a pair of congruent triangles in the figure, and write down the condition under which they are congruent.

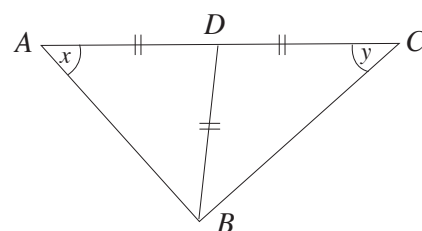


11. Find the least common multiple of  $x(x + 1)$  and  $x^2$ .

12. The figure shows the rectangular lamina that is obtained when a hollow cylinder of height 10 cm is cut along a line which is perpendicular to its base. Find the radius of the cylinder. (Take  $\pi = \frac{22}{7}$ )



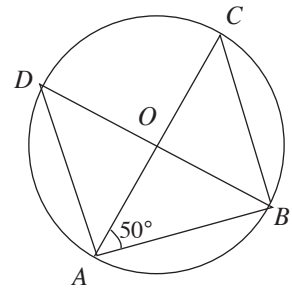
13. Find the value of  $x + y$  based on the information in the given triangle  $ABC$ .



14. Simplify :  $\frac{1}{x} - \frac{1}{3x}$

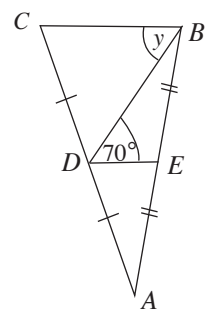
15. The first approximation of the square root of a number is 3.1. What is the perfect square that is closest to this number?

16. In the circle with centre  $O$  shown in the figure,  $\hat{BAC} = 50^\circ$ . Find the magnitude of  $\hat{ADB}$ .

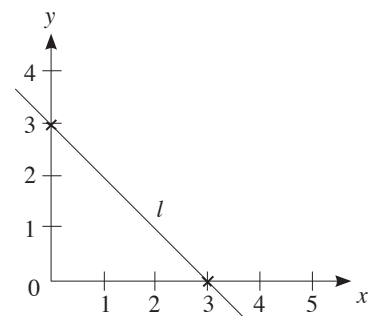


17.  $A = \begin{pmatrix} 3 & -2 \\ -1 & 0 \end{pmatrix}_{2 \times 2}$  and  $I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}_{2 \times 2}$ . Find the matrix  $B$  such that  $2A + B = I$ .

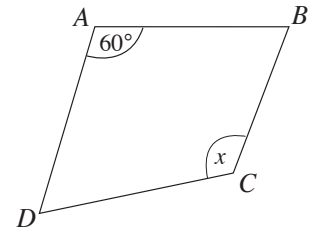
18. Find the value of  $y$  based on the information in the figure.



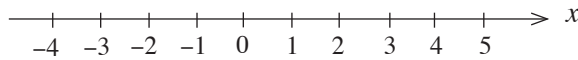
19. Write the equation of the straight line denoted by  $l$  in the figure.



20.  $ABCD$  in the figure is a cyclic quadrilateral. Find the value of the angle denoted by  $x$ .



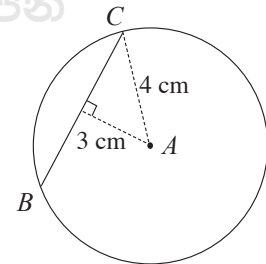
21. Mark the interval of solutions which satisfy both the inequalities  $x \geq -2$  and  $x < 3$  on the given number line.



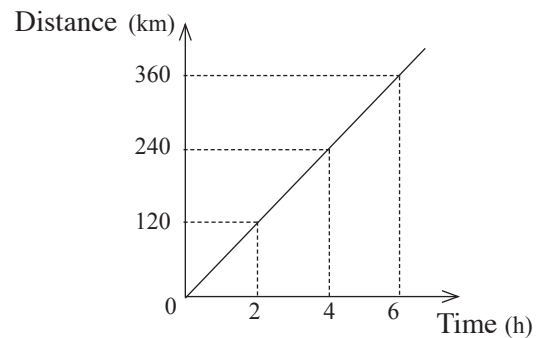
22. Find the common ratio of the geometric progression with first term 3 and fourth term 24.

23. Nine men require 8 days to complete a task. How many days will four men take to complete exactly half this task?

24. Complete the sketch that has been drawn to find the points which are 4 cm from the point  $A$  and 6 cm from the line  $BC$  and name these points as  $D$  and  $E$ .



25. The figure shows the distance time graph relevant to the motion of a vehicle travelling with uniform speed. Find the speed of the vehicle.



\* \*

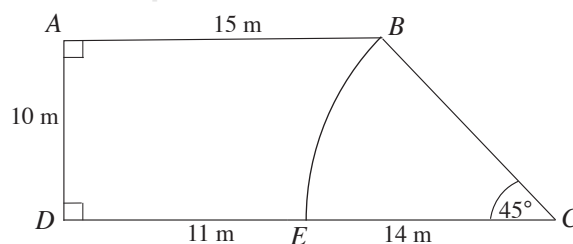
### Part B

Answer **all** questions on this question paper itself. Each question carries 10 marks.

1. Of the letters that a post office received on a certain day,  $\frac{1}{8}$  were registered letters and  $\frac{2}{3}$  were ordinary letters.
- (i) Find the number of registered letters and ordinary letters that were received as a fraction of the total number of letters that were received by the post office that day.
- (ii)  $\frac{1}{5}$  of the remaining letters were express letters. Find the number of express letters that were received as a fraction of the total number of letters.
- (iii) If the remaining letters, which were neither registered letters nor ordinary letters nor express letters were all foreign letters, and if this number was 520, then how many registered letters were received that day?
- (iv) Find the ratio of the ordinary letters to the express letters that were received that day.

2. The figure shows a playground  $ABCD$ . Sand is spread in the section  $BCE$  which is a sector of a circle with central angle  $45^\circ$ . (Take  $\pi = \frac{22}{7}$ )

- (i) Find the perimeter of the section  $ABED$ .

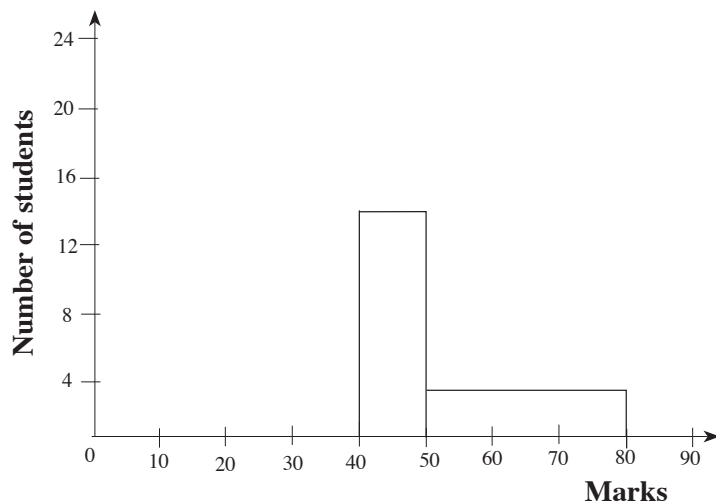


- (ii) Find the area of the section in which sand is spread.
- (iii) Find the area of the section apart from that in which sand is spread.
- (iv) It is required to allocate a section within this playground for a milk stall. Its area should be  $\frac{1}{6}$  of the area of the section apart from that in which sand is spread and it should take the shape of a right angled triangle with  $AD$  as one boundary and another boundary on  $DC$ . On the given figure, mark the section that should be allocated for the milk stall, together with the measurements.

3. (a) The annual assessed value of the building in which the business “Sesiri” is conducted is Rs. 75 000. The urban council charges it Rs. 1500 as rates for a quarter.
- (i) Find the rates that have to be paid for a year, and calculate the annual rates percentage.
  
  - (ii) A discount of 10% is received if the rates for the whole year is paid before the 31<sup>st</sup> of January of that year. Find how much the businessman who owns the building saves, if he pays the rates for the whole year before this date.
- (b) Mr. Silva invested Rs. 270 000 to buy shares of a company which pays Rs. 2 per share as dividends, at a time when the market price of a share of this company was Rs. 9.
- (i) Find the dividends income received by Mr. Silva at the end of a year.
  
  - (ii) After receiving the dividends, if Mr. Silva sold all the shares at the current market price of Rs. 10.50 per share, find his capital gain.

4. The incomplete frequency distribution and corresponding incomplete histogram given below have been prepared with the marks obtained by a group of grade 12 students who participated in a project evaluation. (20 – 30 means more than 20 but less than or equal to 30)

Marks	Number of students
0 – 20	4
20 – 30	10
30 – 40	20
40 – 50	.....
50 – 80	.....

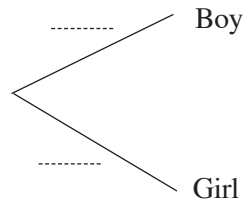


- (i) Complete the frequency distribution using the information in the incomplete histogram.
- (ii) Complete the histogram using the information in the frequency distribution.
- (iii) Draw the frequency polygon on the histogram.
- (iv) It was decided to give a special training to those who have obtained more than 50 marks. Express the number of students who are selected for the training as a percentage of the number of students who participated in the project evaluation.

5. Four boys and 2 girls who are able to sing as well as play a musical instrument are to participate in a talent show. The four boys have been given the numbers 1, 2, 3 and 4 while the two girls have been given the numbers 5 and 6, to select the order in which they are to perform. These six numbers are marked on six identical cards such that each card has a different number. A card is picked at random from the box. The child who has the number which is picked has to sing.

(a) (i) Complete the given incomplete tree diagram.

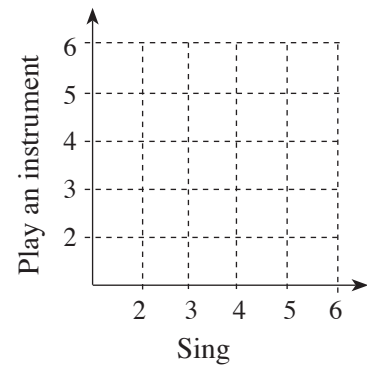
First picking (Sing)



(ii) The first card picked is replaced in the box and again a card is picked at random. The child with this number has to play an instrument. Extend the given tree diagram in a suitable way, and find the probability of a boy performing on one occasion and a girl on the other occasion.

(b) Now suppose that the boy who received the number 1 had to withdraw from the show due to another commitment. If the card with the number 1 is removed from the box and children are picked in the same manner as above from the remaining cards, to sing and to play an instrument,

(i) represent the sample space relevant to picking a child to sing and a child to play an instrument in the given grid.



(ii) Mark the event of the same child not being picked to sing and play an instrument on the grid and find its probability.

\* \* \*

# G.C.E.(O.L.) Support Seminar - 2016

## Mathematics II

Three hours

- \* Answer **ten** questions, selecting **five** questions from **Part A** and five questions from **Part B**.
- \* Each question carries 10 marks.
- \* The volume of a right circular cone with base radius  $r$  and height  $h$  is  $\frac{1}{3}\pi r^2 h$ .

### Part A

Answer only **five** questions.

1.  $A$  and  $B$  are two financial institutions which provide loans as follows.

#### Institution A

- Charges interest at an annual interest rate of 18%.
- Interest is calculated on the reducing balance.
- The loan amount and interest have to be paid in equal monthly installments.

#### Institution B

- Charges interest at an annual interest rate of 10% and the interest is compounded annually.
- The loan amount and the total interest have to be paid together at the end of the loan period.

Samantha needs to obtain a loan of Rs. 300 000. He intends to settle the loan together with the interest by the end of two years. Samantha's friend says that more interest has to be paid if the loan is taken from Institution A. Find the total interest that has to be paid when this loan amount is taken from each of these two institutions, and with reasons explain the truth / falsehood of the friend's statement.

2. The table below gives the  $y$  values of the function  $y = (x + 1)(x - 3)$  corresponding to several given  $x$  values.

$x$	-1	0	1	2	3	4	5
$y$	0	-3	-4	-3	0	....	12

- (a) (i) Find the value of  $y$  corresponding to  $x = 4$ .  
(ii) Draw the graph of the above function by selecting a suitable scale.
- (b) By using the graph,  
(i) find the minimum value of the function.  
(ii) explain the behavior of the graph on the interval  $-1 < x < 1$ , by indicating whether it is positive or negative and whether it is increasing or decreasing.
- (c) By drawing a suitable straight line graph on the above coordinate plane, obtain a value for  $\sqrt{3}$  to the nearest first decimal place.

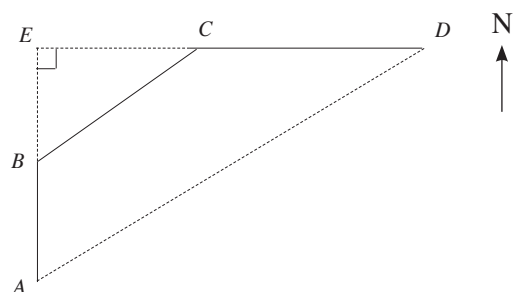


3. The frequency distribution of the number of trips made during a day by 40 vehicles of the same type transporting soil to the construction site of a expressway is given below.

Class Interval (Number of trips)	4 - 8	9 - 13	14 - 18	19 - 23	24 - 28	29 - 33	34 - 38
Frequency (Number of vehicles)	2	3	5	8	15	5	2

- How many vehicles made more than 33 trips transporting soil?
  - Find the mean number of trips that a vehicle makes during a day transporting soil, to the nearest whole number.
  - Each vehicle can carry 4 cubes of soil per trip. If the price of one cube of soil is Rs. 2000, what is the expected cost of the soil that is transported during a day by one vehicle?
  - The engineer states that since all the above vehicles would have to be used for 2 days to transport the soil required for a length of 100 m of the highway, the cost of the soil for this would exceed 14 million rupees. Give reasons to show that his statement could be true.
4. The government provides aid of Rs. 100 per child and Rs. 150 per adult daily for those sheltering in a certain camp due to being displaced by floods. On a certain day, a group of students brought 31 apples, cut into 6 pieces each, and 29 guavas cut into 4 pieces each to be distributed among the displaced in the camp. When the children were provided with 3 pieces of apple each and the adults with 2 pieces each, and the children were provided with 2 pieces of guava each and the adults with 1 piece each, only 2 pieces of guava were left over. Find the number of children and the number of adults among the displaced in this camp and hence find the total amount of money the government needs to give for a week to the displaced in this camp.
5. The length of the hypotenuse of a right angled triangle is 1 cm less than twice the length of its shortest side.
- If the length of the shortest side is  $x$  cm, express the length of the hypotenuse in terms of  $x$ .
  - If the remaining side is 3 cm more than the length of the shortest side, using Pythagoras' theorem, write down a relationship between the squares of the lengths of the sides of the triangle.
  - Show that by simplifying the above relationship the equation  $x^2 - 5x = 4$  is obtained.
  - Find the length of the hypotenuse by solving the above equation using the method of completing the square or by using the formula. (Take  $\sqrt{41} = 6.4$ )

6. Starting from the location  $A$ , Kamal travels 12 metres to the North and arrives at the location  $B$  as shown in the figure. From  $B$  he travels 20 metres on a bearing of  $040^\circ$  and arrives at the location  $C$ , and from  $C$  he travels 25 metres to the East to reach the location  $D$ .



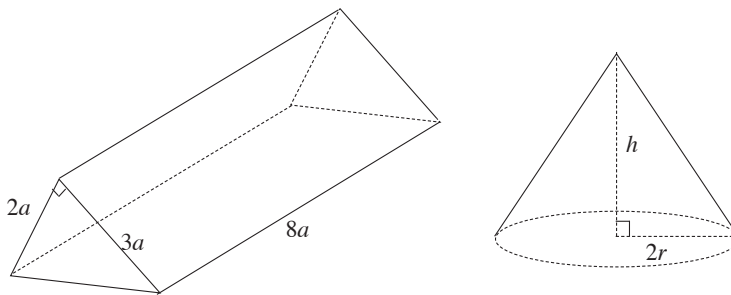
- Copy the above figure, and mark the given information in it.
- Find the distance  $CE$  to the nearest metre using the trigonometric tables.
- The distance  $BE$  rounded off to the nearest metre is 15 m. Accordingly, calculate  $\hat{EAD}$  and the distance  $AD$ .

**Part B**

Answer only **five** questions.

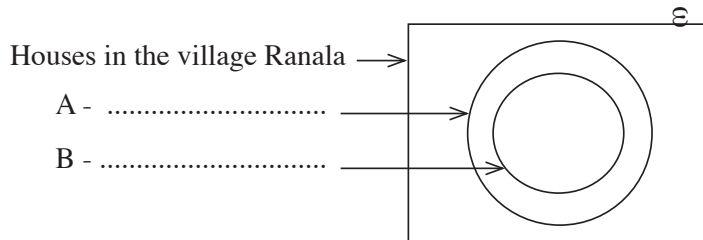
7. A competitor participating in the programme “Wasanavanthaya” organized by a certain television channel, wins by answering 15 questions correctly. The prize money of Rs. 50 for the first question, Rs. 75 for the second question, Rs. 100 for the third question etc., given for the correct answers, are in an arithmetic progression.
- (i) Find the prize money allocated for the 12<sup>th</sup> question.
  - (ii) If Rs. 425 has been allocated as prize money for 2 consecutive questions, which 2 questions are they?
  - (iii) A competitor has to leave the program if a wrong answer is given. In this case, the competitor’s prize money is half the amount allocated for all the questions he has answered correctly thus far. If a certain competitor had to leave the competition with Rs. 1300 due to not giving the correct answer to a certain question, show that the number of questions he answered is 14.
8. Using only a straight edge with a cm/mm scale and showing the construction lines clearly, do the following constructions.
- (i) Construct a straight line segment  $PQ$  of length 8 cm.
  - (ii) Mark the point  $R$  such that  $\hat{QPR} = 45^\circ$  and  $PR = QR$ , and complete the triangle  $PQR$ .
  - (iii) Construct the circle that passes through the points  $P, Q$  and  $R$  and name its centre  $O$ .
  - (iv) Mark the point  $S$  on  $PR$  produced such that  $PR = RS$ .
  - (v) Mark the point  $T$  on the circle such that  $SQ = ST$  and show that  $SQ$  and  $ST$  are two tangents to the circle.

9.



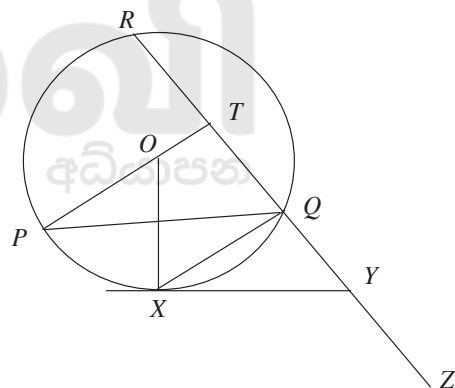
The above figure shows a solid metal right prism with a right triangular cross section, and a solid right circular cone. Their measurements have been given in the figure in the same units. The solid cone with base radius  $2r$  and height  $h$  is made with the metal that is obtained by melting the prism, such that there is no waste. Show that when the height of the cone is 15 cm,  $r^2 = \frac{6a^3}{5\pi}$ . By taking  $\pi = 3.14$  and using the logarithms table, find the value of  $r^2$  when  $a = 4.55$  cm, and hence find the radius of the cone.

10. There are 120 houses in the village Ranala. 113 of these houses have television sets. Of the houses which have television sets, 78 do not have radios. Every house that has a radio has a television set too.



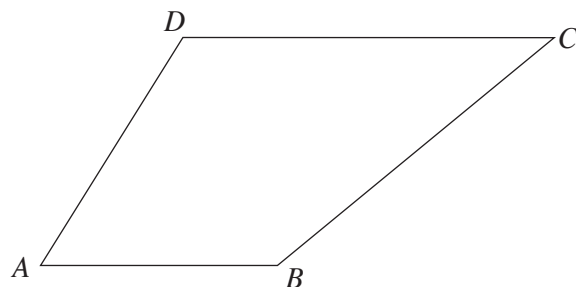
- (i) Identify the sets A and B and complete the Venn diagram using the given information.
- (ii) How many houses have both a television set and a radio?
- (iii) What is the probability of a house picked at random from the houses in the village Ranala being one which does not have a radio?
- (iv) None of the houses in the village Ranala have computers. A private institution decides to provide computers to 25 selected houses in this village. If they select 4 houses which do not have television sets and 9 houses which have radios to be among the houses which receive the computers, draw the Venn diagram again to represent this information, taking C to be the set of houses which are provided with computers.
- (v) Now, shade the region in the Venn diagram which denotes the set of houses which do not have radios but have television sets and computers.

11.  $PQ$  and  $QR$  are two chords of the circle with centre  $O$  shown in the figure.  $PO$  produced bisects  $RQ$  at  $T$ . The tangent drawn to the circle at  $X$  is  $XY$ . The chord  $RQ$  has been produced to  $Z$  and  $\hat{POX} = 40^\circ$ .



- (i) Giving reasons, write the magnitude of  $\hat{PQX}$ .
- (ii) Show that  $OTYX$  is a cyclic quadrilateral.
- (iii) Find the magnitude of  $\hat{XYZ}$ .
- (iv) Name a diameter of the circle passing through the points  $O, T, Y$  and  $X$ , and write the theorem which is the reason for it.

12. In the quadrilateral  $ABCD$  shown in the figure, the points  $E$  and  $F$  lie on the side  $CD$  such that  $CE = EF = FD$ .  $AF$  and  $BE$  produced meet at  $G$  such that  $AF = FG$  and  $BE = EG$ . Sketch a figure with this information marked in it. Show that  $BCGF$  and  $ABCF$  are parallelograms and that they are equal in area.



\* \* \*

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## எங்கள் குறிக்கோள்

எண்ணிம உலகத்தில் மாணவர்களிற்கென சிறந்ததொரு கற்றல் கட்டமைப்பை உருவாக்குதல்.

அனைத்தும் டிஜிட்டல் மயப்படுத்தப்பட்ட இந்த காலத்தில் பல்வேறு துறைகளும் கால ஓட்டத்துடன் இணைந்து டிஜிட்டல் தளத்தில் பல்கிப்பெருகி வருகின்றன. அந்த வகையில் கல்வித்துறையும் இதற்கு விதிவிலக்கல்ல. இணையவழி கல்வியின் மூலம் கல்வித்துறை புதியதொரு பரிமாணத்தை எட்டியுள்ளது. குறிப்பாக கொரோனா பேரிடர் காலத்தில் நாடே முடக்கப்பட்டிருந்தது. இதனால் மாணவர்களிற்கும் பாடசாலை, கல்வி நிறுவனங்களிற்கு இடையிலான தொடர்பு துண்டிக்கப்பட்டது. அந்த இக்கட்டான சூழ்நிலையில் இணையவழி வகுப்புகள் மாணவர்களிற்கு வரப்பிரசாதமாக அமைந்தது என்பதே உண்மை.

இன்று தொழில்நுட்பம் மாணவர்களை தவறான பாதைக்கு இட்டு செல்வதாக ஓர் எண்ண ஓட்டம் மக்கள் மத்தியில் உள்ளது. தொழில்நுட்பம் என்பது ஒரு கருவி மட்டுமே அதை எவ்வாறு பயன்படுத்துகிறோம் என்பதில் அதன் ஆக்க மற்றும் அழிவு விளைவுகள் தீர்மானிக்கப்படுகிறது. உளியை கொண்டு சிலையை செதுக்க நினைத்தால் அவன் நிச்சயம் சிற்பி ஆகலாம். இங்கு பிரச்சினையாக காணப்படுவது மாணவர்களை வழிப்படுத்த தொழில்நுட்ப உலகில் ஓர் முறையான கட்டமைப்பு இல்லாமையே. அதை உருவாக்குவதே எங்கள் நோக்கம். அதை நோக்கியே எங்கள் பயணம் அமையும்.

**எமது இணையத்தினூடக ஊடக உங்களிற்கு தேவையான பரீட்சை வினாத்தாள்களை இலகுவான முறையில் தரவிறக்கம் செய்து கொள்ளமுடியும்.**

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**கல்வி சார் செய்திகளை உடனுக்குடன் அறிந்து கொள்ள எமது சமூக ஊடக தளங்களின் ஊடக உடனுக்குடன் அறிந்து கொள்ள முடியும்.**



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